

# Evaluating Encodings for Bivariate Edges in Adjacency Matrices

Jorge Acosta-Hernández, Alexander Lex, Tingying He

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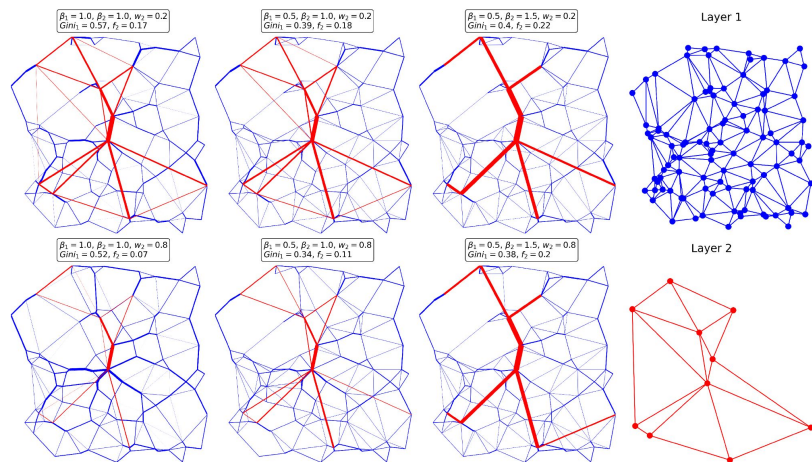
visualization  
design lab

# Multivariate networks occur in many real-world domains

Multilayer social networks reveal the social complexity of a cooperatively breeding bird

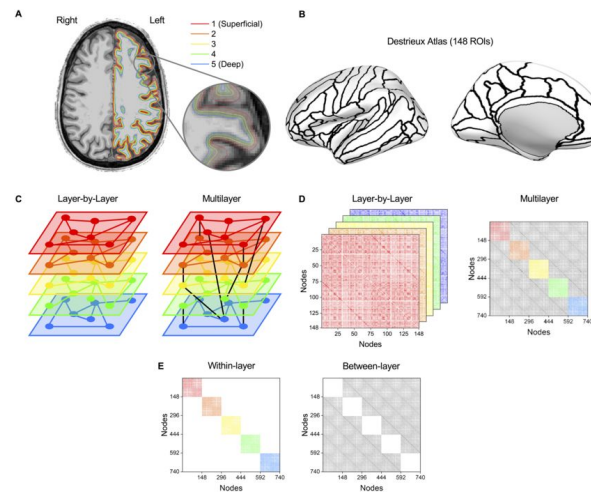
## Optimal Transport in Multilayer Networks for Traffic Flow Optimization

Abdullahi Adinoyi Ibrahim \*<sup>1</sup>, Alessandro Lonardi \*<sup>2</sup> and Caterina De Bacco \*<sup>3</sup>



## Multilayer network analysis across cortical depths in 7-T resting-state fMRI

Parker Kotlarz<sup>1,2</sup>, Kaisu Lankinen<sup>1,3</sup>, Maria Hakonen<sup>1,3</sup>, Tori Turpin<sup>4</sup>, Jonathan R. Polimeni<sup>1,3,5</sup>, and Jyrki Ahveninen<sup>1,3</sup>

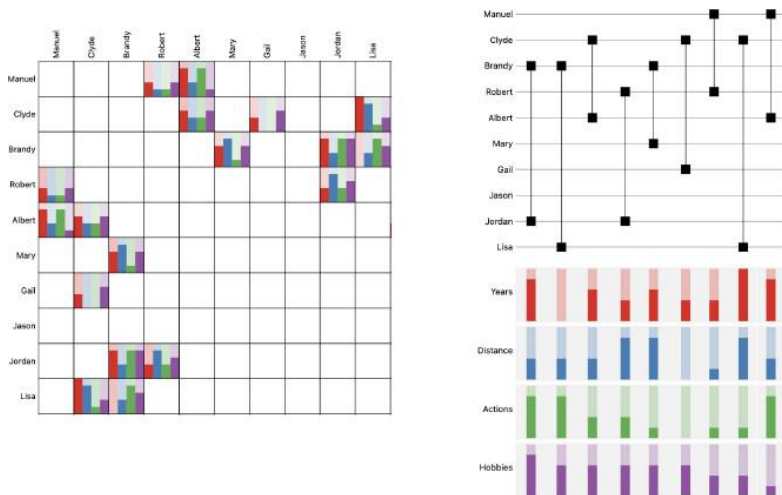


# Prior work have explored MVN AMs encodings

## Exploring the Design Space of BioFabric Visualization for Multivariate Network Analysis

J. Fuchs<sup>1</sup> , F. L. Dennig<sup>1</sup> , M.-V. Heine<sup>1</sup> , D. A. Keim<sup>1</sup>  and S. Di Bartolomeo<sup>1</sup> 

<sup>1</sup>University of Konstanz, Germany



## Weighted Graph Comparison Techniques for Brain Connectivity Analysis

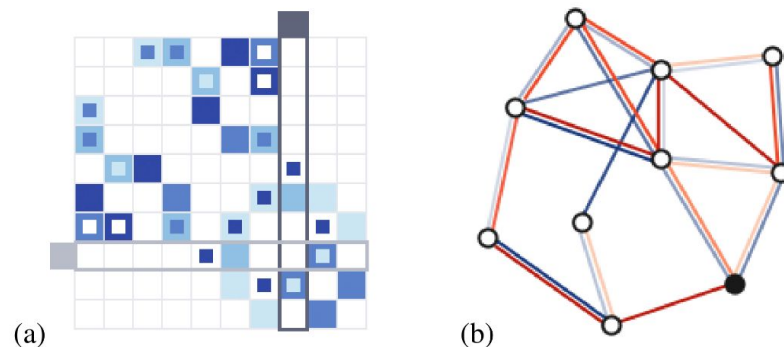
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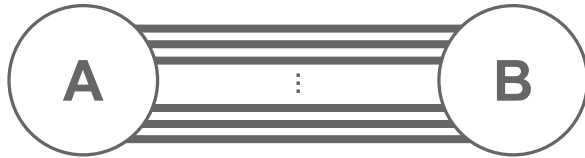
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# What if we add more attributes?

## 1. Many edge attributes



Attribute1	40
Attribute2	125
Attribute3	75
⋮	
Attribute28	75
Attribute29	170
Attribute30	35

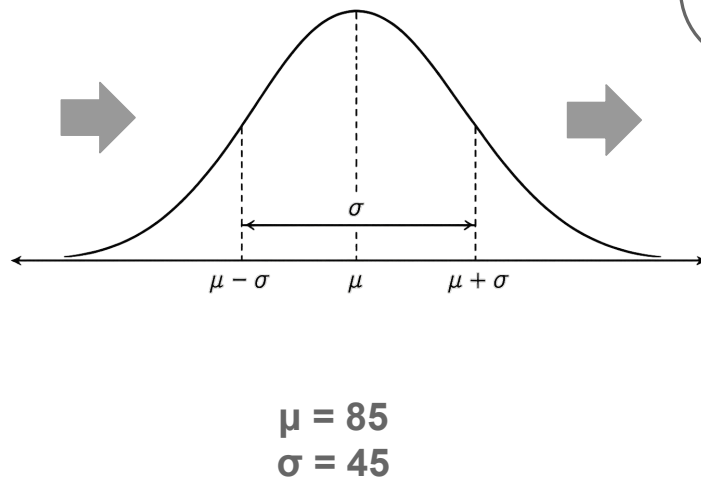
# Our approach

## 1. Many edge attributes

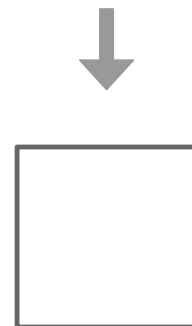


Attribute1	40
Attribute2	125
Attribute3	75
...	
Attribute28	75
Attribute29	170
Attribute30	35

## 2. Summarize

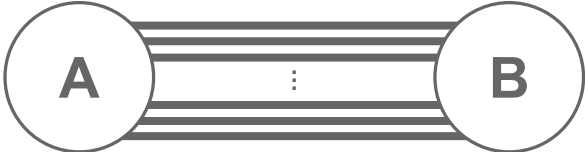


## 3. Encode the summary



# Best technique to encode two quantitative attributes?

1. Many edge values



Attribute1	40
Attribute2	125
Attribute3	75
⋮	
Attribute28	75
Attribute29	170
Attribute30	35

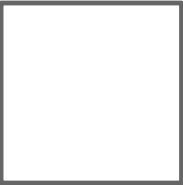
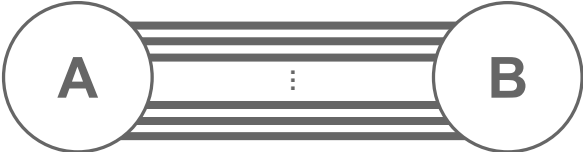
2. Summarize them



$$\mu = 55$$
$$\sigma = 20$$



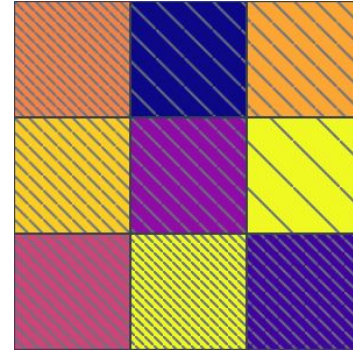
3. Encode two values



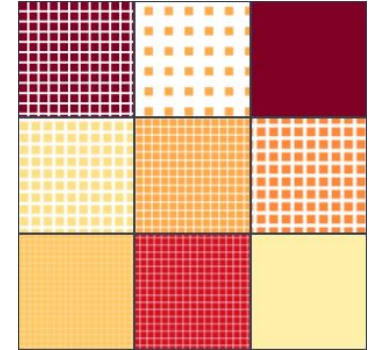
# Design Space Characterization

# The cell as a whole

- Cell is the only visual mark
- Attributes encoded through properties of the cell
- Compact design, limited perceptual separability



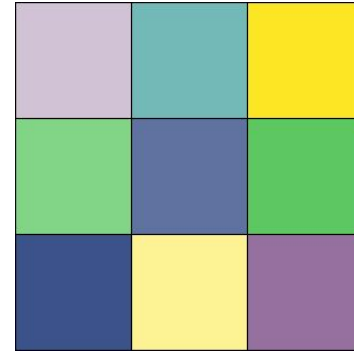
Hue & Hatching



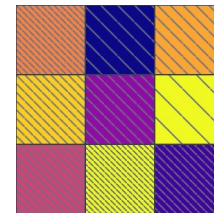
Hue & Squares

# Technique selection - The cell as a whole

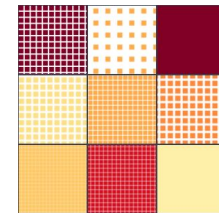
- Selected technique:
  - **Bivariate Color**
- Mean = Hue
- Standard deviation = Lightness
- Common and Visually compact



Hue & Lightness



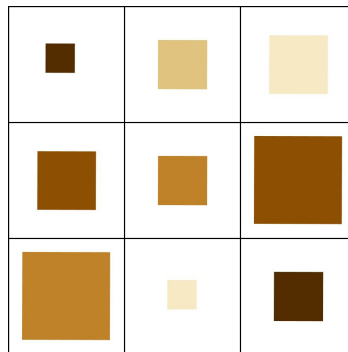
Hue & Hatching



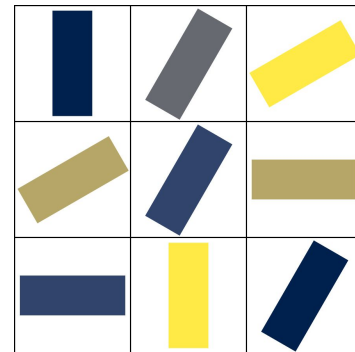
Hue & Squares

# One overlaid mark

- Adds one mark inside each cell
- One attribute can use the cell, while other uses the added mark
- Both attributes encoded by the added mark
- Balance compactness and separation



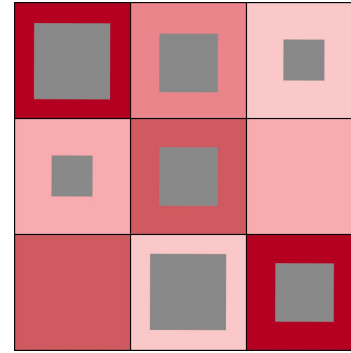
Mark Hue & Size



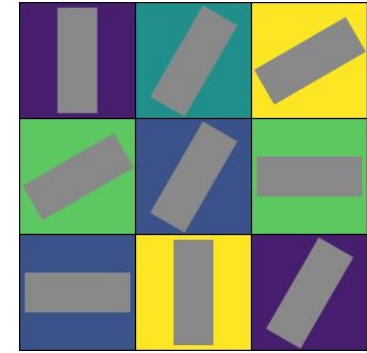
Mark Hue & Angle

# Technique selection - One overlaid mark

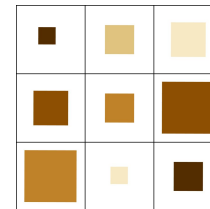
- Selected techniques:
  - **Mark angle**
  - **Mark Size**
- Same strategy, different mark channel
- Tests the effect of the mark channel



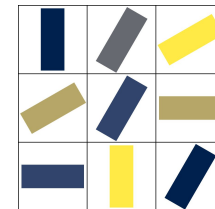
Hue & Mark Size



Hue & Mark Angle



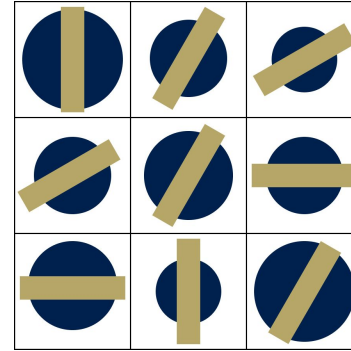
Mark Hue & Size



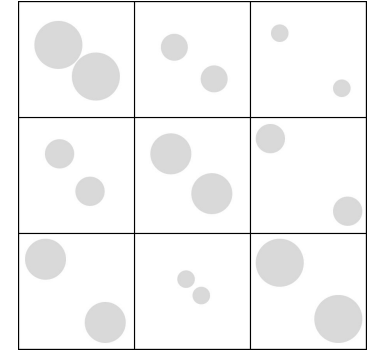
Mark Hue & Angle

# Two overlaid marks

- Adds two marks inside each cell
- Each mark is assigned to one edge attribute
- The cell as a neutral container
- Supports separability, but increases within-cell complexity



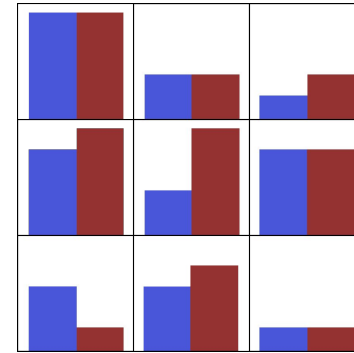
Mark Radius &  
Mark Angle



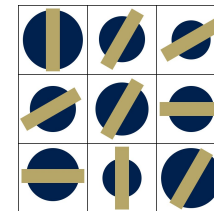
Mark Radius &  
Mark Position

# Technique selection - Two overlaid marks

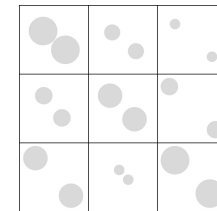
- Selected technique:
  - **Embedded bars**
- Already used
- Strong channel
- Good separation between attributes



Bars



Mark Radius &  
Mark Angle



Mark Radius &  
Mark Position

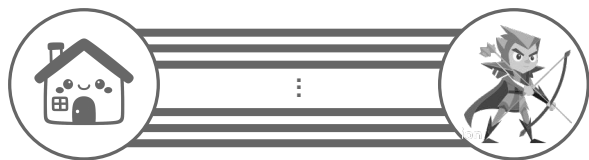
# Evaluation Study Design

# Research Questions

- RQ1: How do the selected edge encoding techniques compare in **task performance** on common MVN tasks?
  - 8 MVN tasks
  - Structural, Attribute and Estimation tasks
- RQ2: How do the selected edge encoding techniques compare in **perceived readability**?
  - PREVis scale 4 constructs measured with 7-point Likert scales
- RQ3: How do the selected edge encoding techniques compare in **perceived aesthetics**?
  - BeauVis scale 5 concepts measured with 7-point Likert scales

# Data: Airline Fares

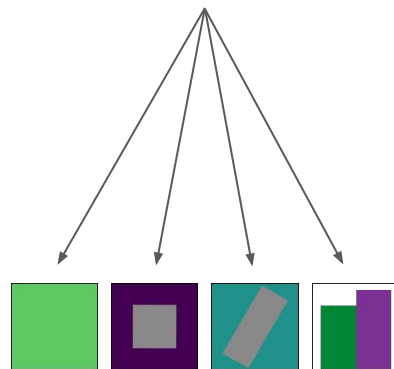
- Real-world data, ecological validity
- Sufficiently dense and attribute-rich networks
- Familiar topic



	\$20
	\$75
	\$40
	\$55

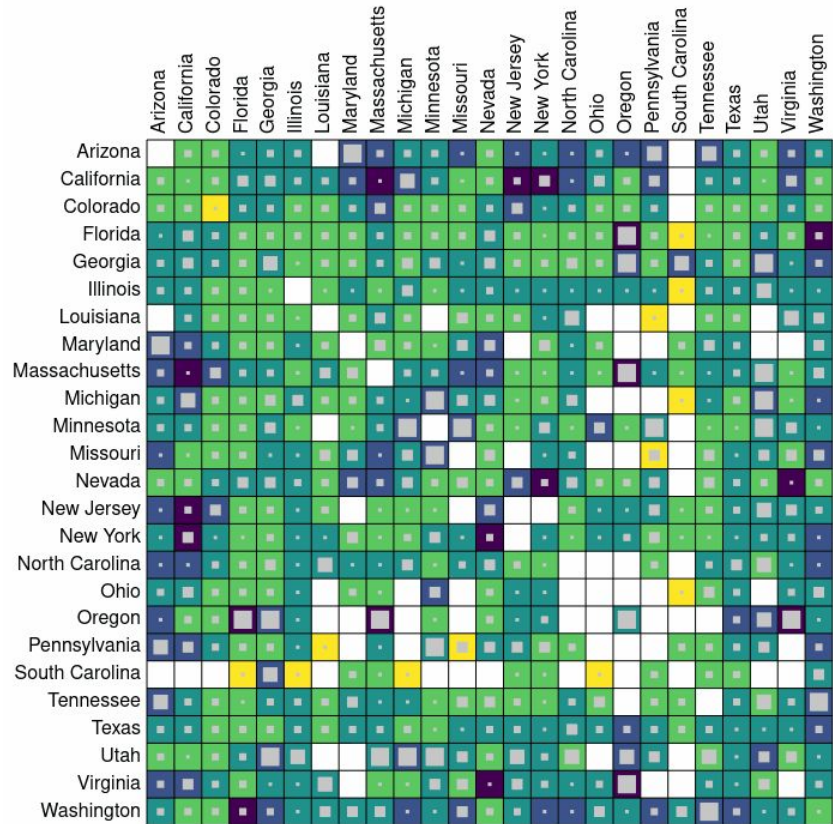


$$\mu = 55$$
$$\sigma = 20$$



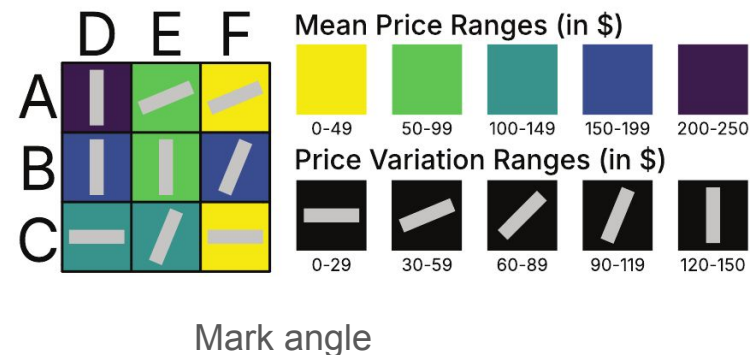
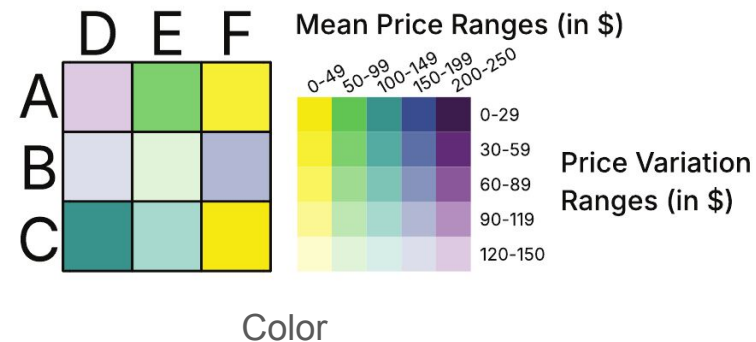
# Stimuli Design

- Matrix size:
  - 25 nodes
  - Network density = 0.7
  - 23 × 23 px cells



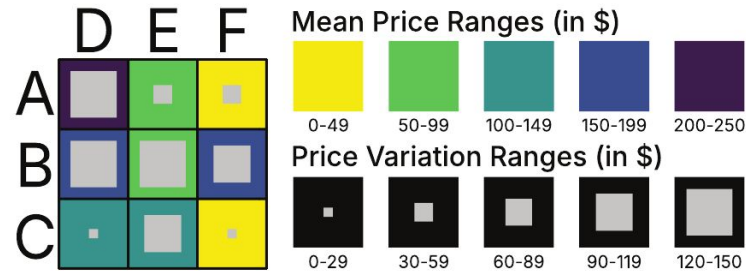
# Stimuli Design

- Matrix size:
  - 25 nodes
  - Network density = 0.7
  - 23 × 23 px cells
- Viridis:
  - Perceptually uniform multihue scale
  - Robust for color-vision deficiencies

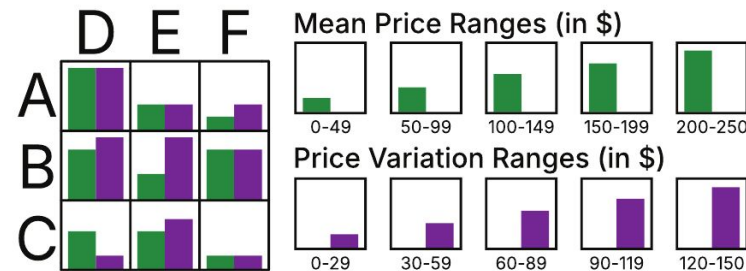


# Stimuli Design

- Matrix size:
  - 25 nodes
  - Network density = 0.7
  - 23 × 23 px cells
- Viridis:
  - Perceptually uniform multihue scale
  - Robust for color-vision deficiencies
- 5 interpretable ranges:
  - Simple and interpretable



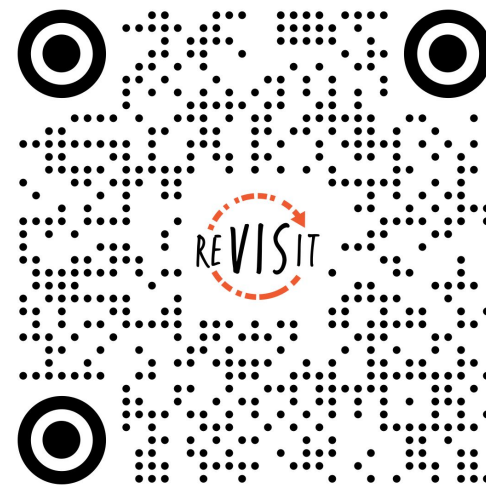
Mark size



Bars

# Study Setting

- Procedure:
  1. Introduction to network data + Questions
  2. Introduction to encoding technique + Training
  3. Multivariate network tasks + Attention checks
  4. Subjective judgements:
    - a. PREVis
    - b. BeauVis
  5. User feedback + demographics
- Between Subjects with 156 participants
- Implemented with reVISit



<https://tinyurl.com/bvnnv-study>

# Example of a Training task

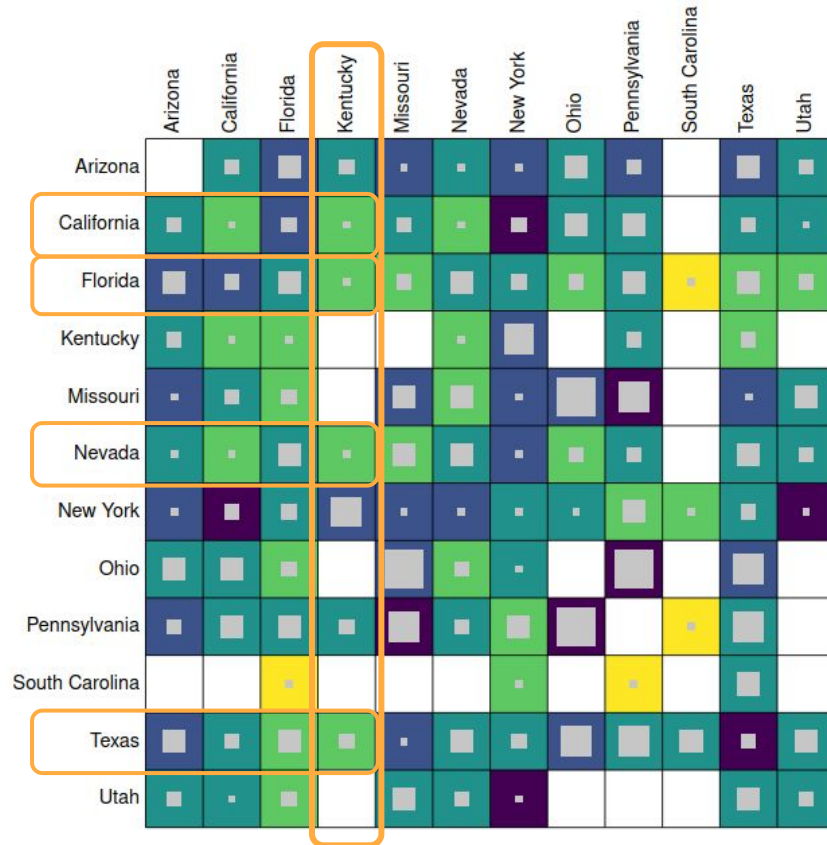
## Task:

Training: Select all states connected to Kentucky with a mean price below \$100.

Selected States: \*

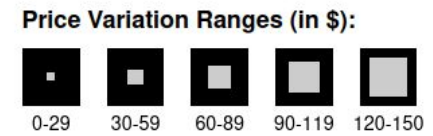
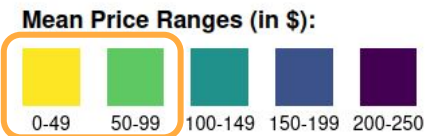
Check Answer

Next



Clear State Selection

Clear Flight Selection



# Example of a Evaluation task

## Task:

Which cluster shows the highest price variation?

Select a cluster: \*

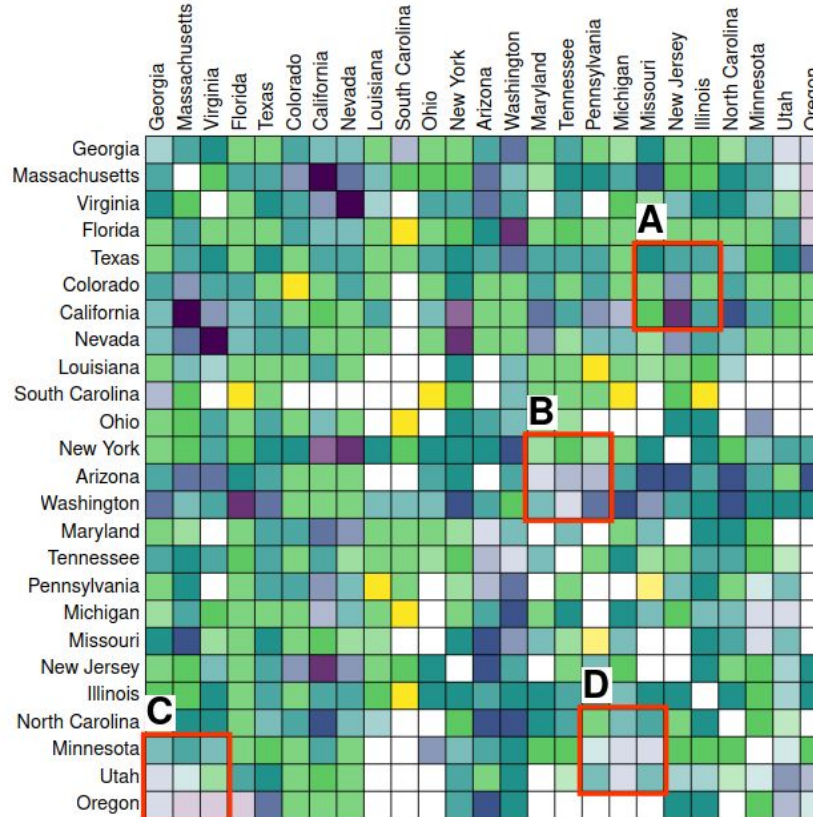
A

B

C

D

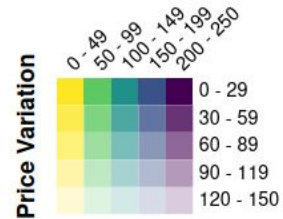
Next



Clear State Selection

Clear Flight Selection

Mean Price Ranges (in \$):

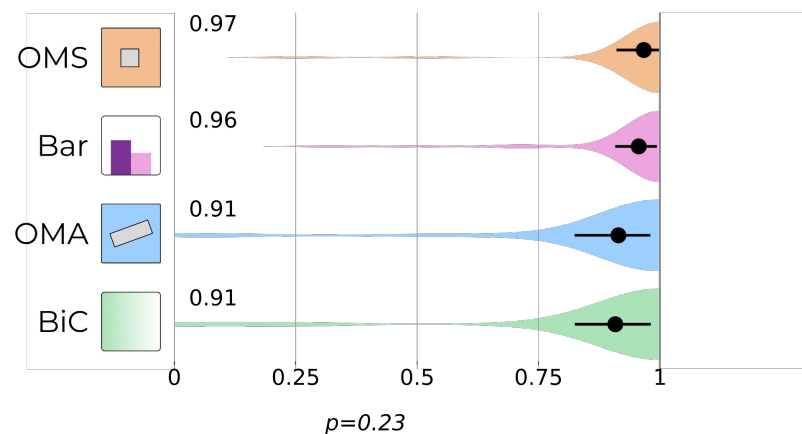


# **Results & Design Implications**

# Encodings don't affect structure

- Performance  $\geq 90\%$  in all conditions
- No significant differences
- All designs preserve basic topology

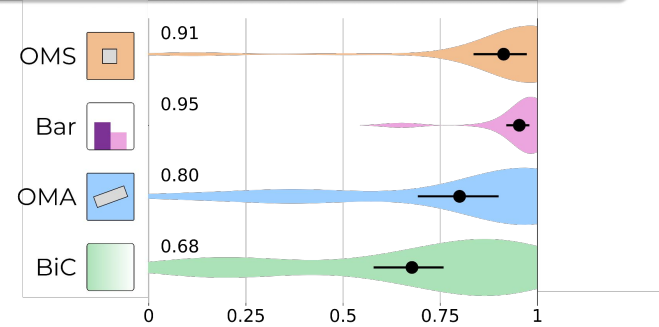
## Structural Adjacency



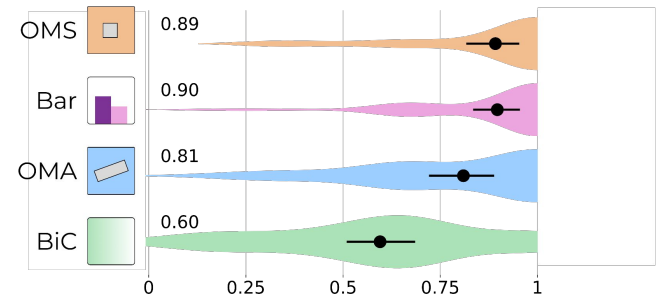
# Mark size and Bars are the top performers

- Top Performance >90% in 6/8 tasks
- Mark Size and Bars perform similarly
- Generally above Mark Angle and Color

Adjacency by Standard Deviation



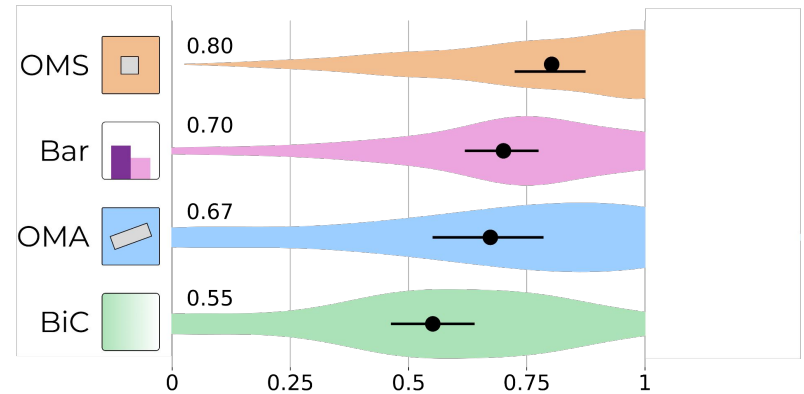
Classification by Standard Deviation



# Extremes are easier to spot with Mark Size

- 10 percentage points above Bars
- Hue + size supports outlier scanning

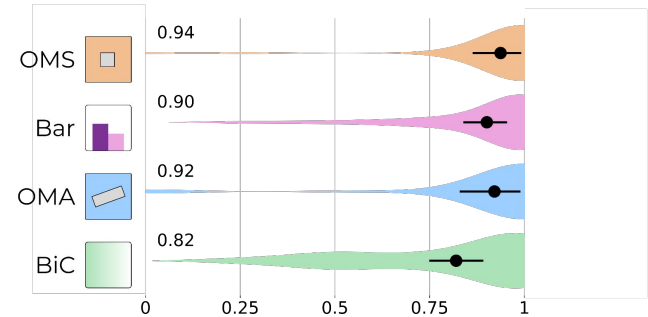
## Extreme Detection



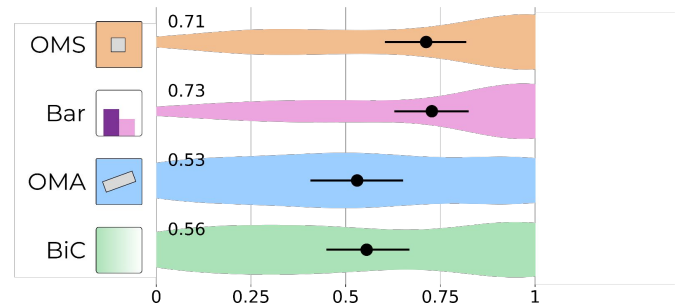
# Performance declines when attributes are combined

- Performance >90% in tasks involving one attribute
- Performance drops 10–20 percentage points in multiattribute tasks
- Combining attributes increases errors

Adjacency by Mean



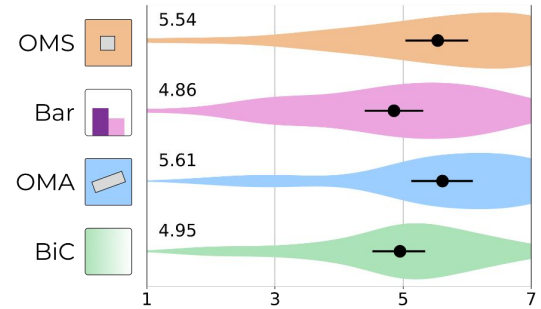
Adjacency by Mean & Standard Deviation



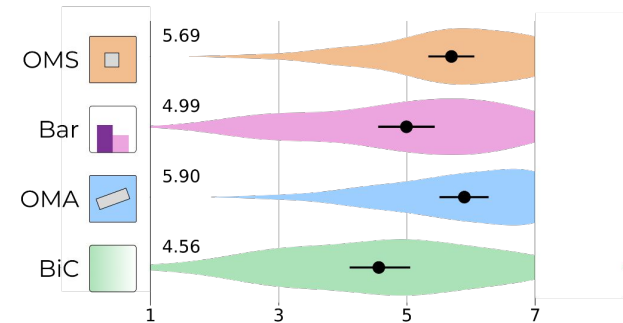
# Perceived Readability

- Single-mark encodings rated highest
- Bars and Color rated lower
- Perceived Readability  $\neq$  Performance

Ability to Read Features (PREVis)



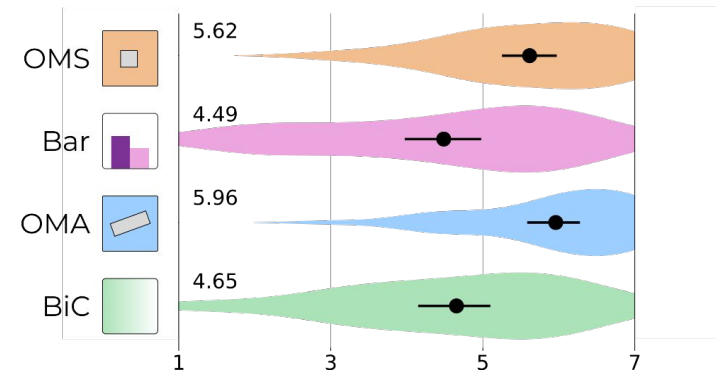
Ability to Read Data (PREVis)



# Perceived Aesthetics

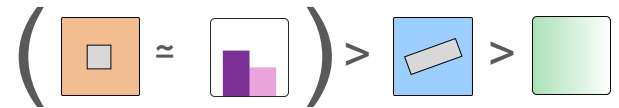
- Single-mark encodings rated highest
- Bars and Color rated lower
- Aesthetics closely aligned with perceived readability

Aesthetics (BeauVis)



# Design guidelines for small-cell dense AMs

- Use Mark size by default
  - Best trade-off between accuracy and user acceptance
- Consider Bars as a strong alternative
  - Competitive performance, but perceived as less readable
- Reserve Mark angle for coarse judgments
  - Strong subjective ratings, less stable accuracy
- Avoid Color for quantitative comparisons
  - Compact, but low separability in small cells



# Evaluating Encodings for Bivariate Edges in Adjacency Matrices

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<https://tinyurl.com/bvnnv-study>



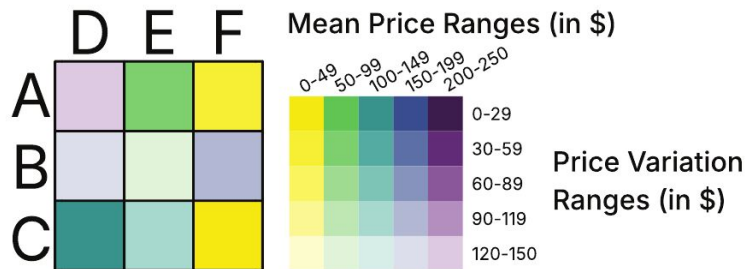
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DE MADRID

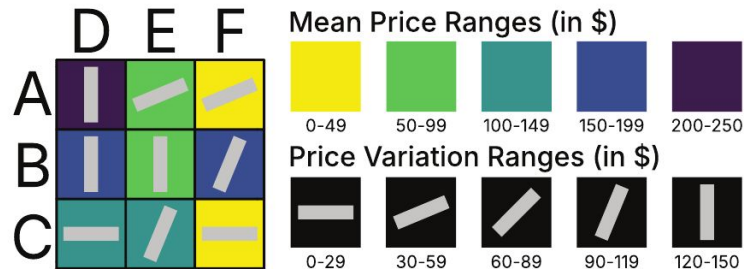


visualization  
design lab

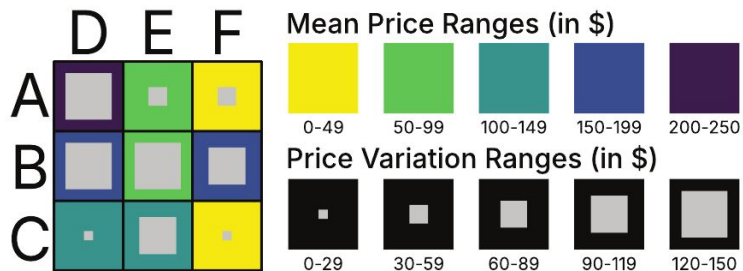
# Stimuli Legends



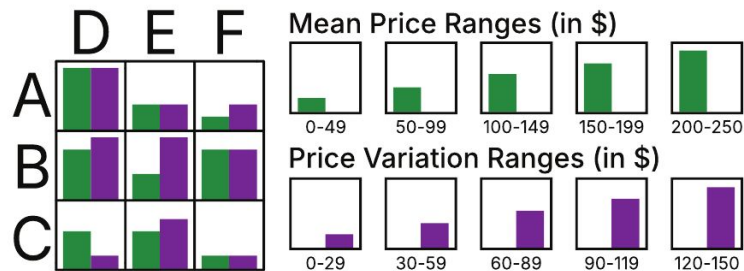
Color



Mark angle

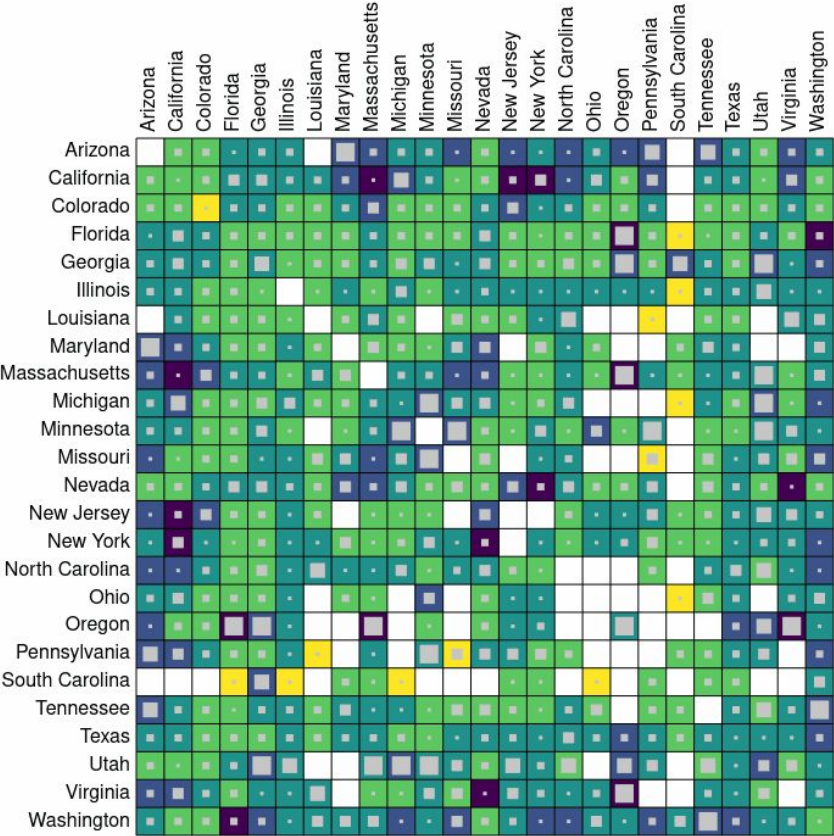


Mark size

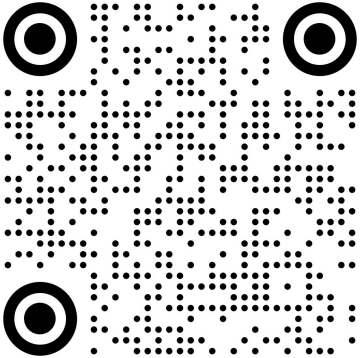


Bars

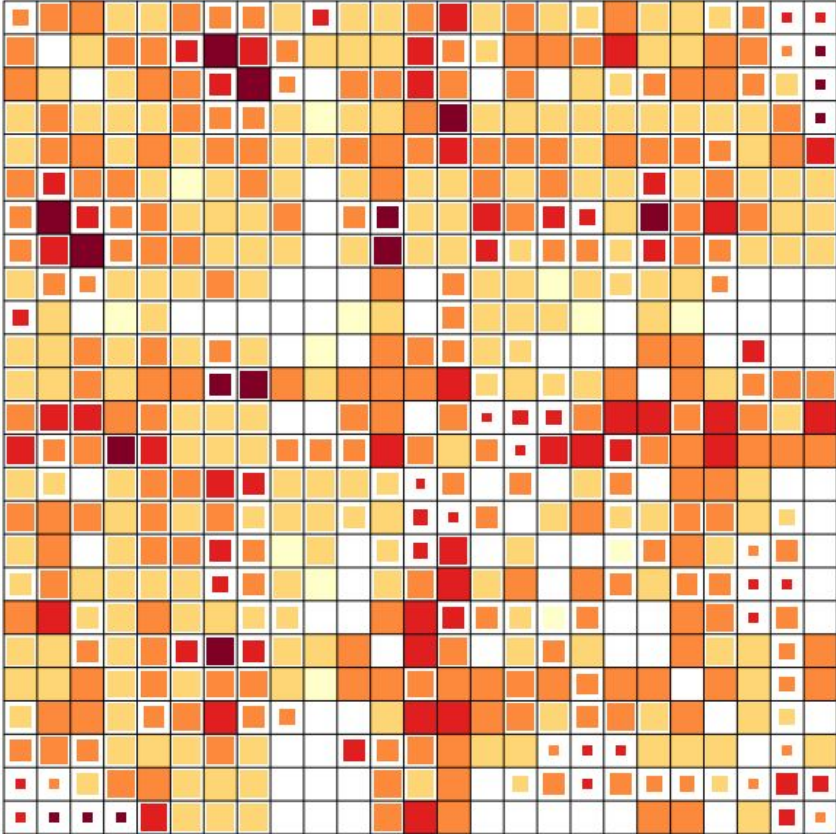
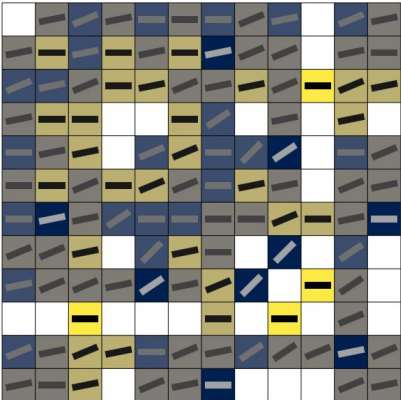
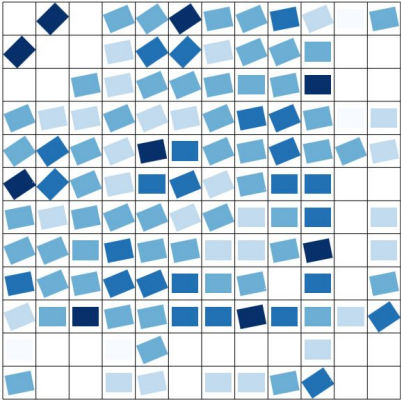
# Stimuli Design



# Experimentation Prototype



<https://tinyurl.com/bvnmv-prototype>

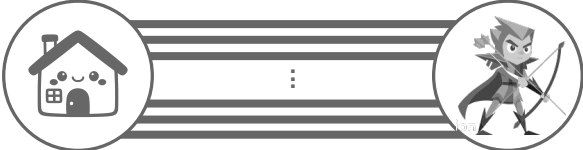


# 156 participants

- Age  $35 \pm 11$
- Experience with AMs  $2.6 \pm 1$
- Gender balanced 78M / 71F / 7
- Education Mode Bachelor

# Data: Airline Fares

## 1. Many fares per route



	\$20
	\$75
⋮	
	\$40
	\$55

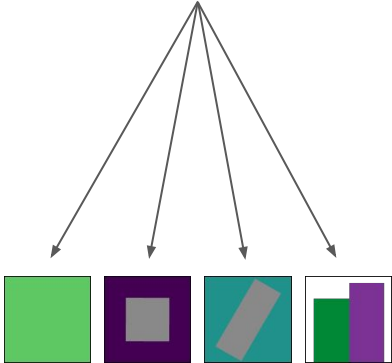


## 2. Summarize distribution

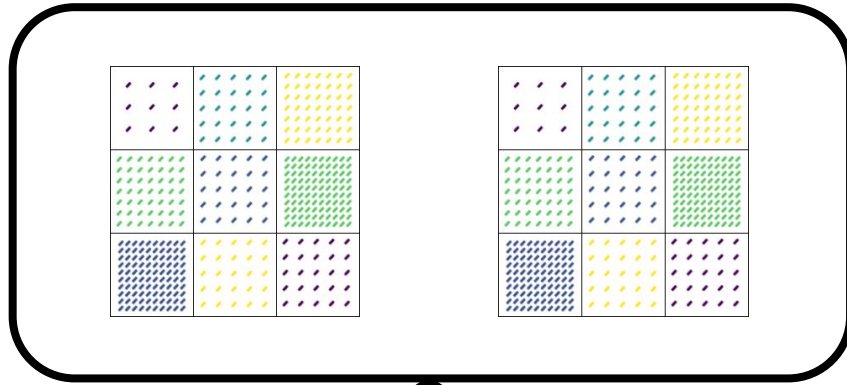
$$\mu = 55$$
$$\sigma = 20$$



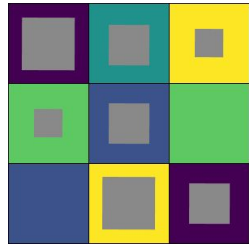
## 3. Encode summaries



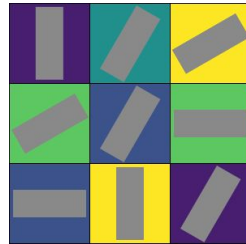
# Technique selection - One overlaid mark



- Same strategy, different channel
- Area, common channel
- Angle might benefit of the grid
- Assess how mark channel affects performance



Mark size

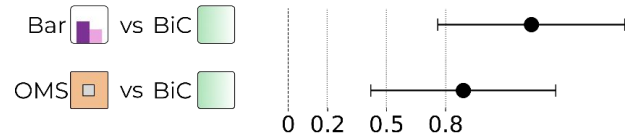


Mark angle

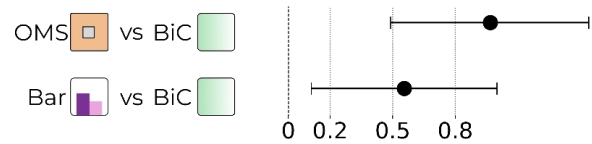
# Bivariate color was the weakest performer

- Lowest performance in 5/8 tasks
- **Weak in dispersion-based tasks**
- Shows **medium to large effects** against top performers

## Adjacency by Standard Deviation



## Extreme Detection

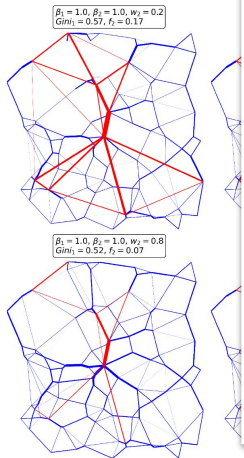


# Multivariate networks occur in many real-world domains

Multilayer social  
complexity of a

## Optimal Transport Flow Optimization

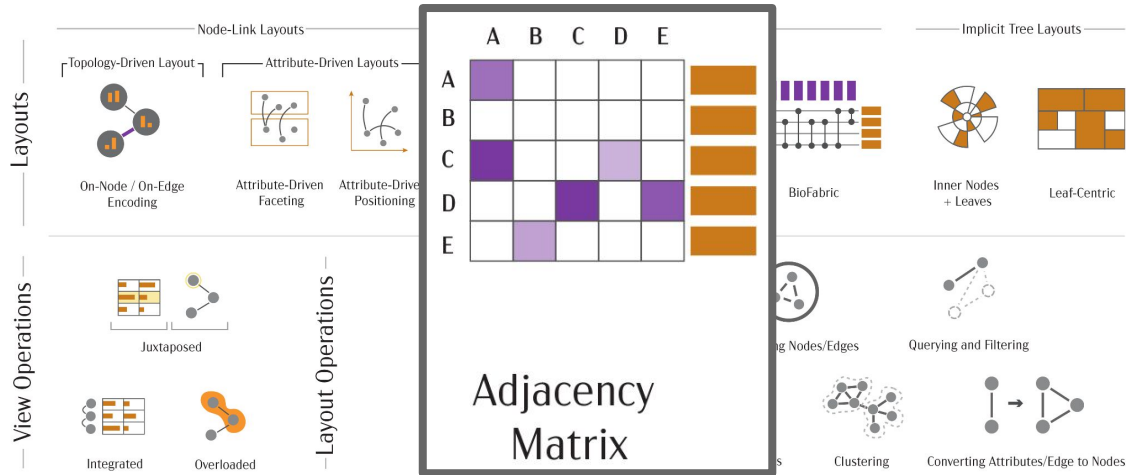
Abdullahi Adinoyi Ibrahim \*



## The State of the Art in Visualizing Multivariate Networks

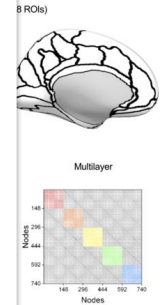
C. Nobre<sup>1</sup>, M. Meyer<sup>1</sup>, M. Streit<sup>2</sup>, and A. Lex<sup>1</sup>

<sup>1</sup>University of Utah, Utah, USA  
<sup>2</sup>Johannes Kepler University Linz, Austria



## cross cortical ate fMRI

en<sup>1,3</sup>, Tori Turpin<sup>4</sup>,  
nenin<sup>1,3</sup>



# Current approaches tested a few attributes

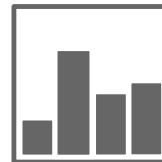
## 1. Edge attributes



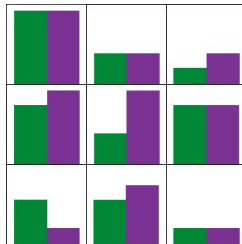
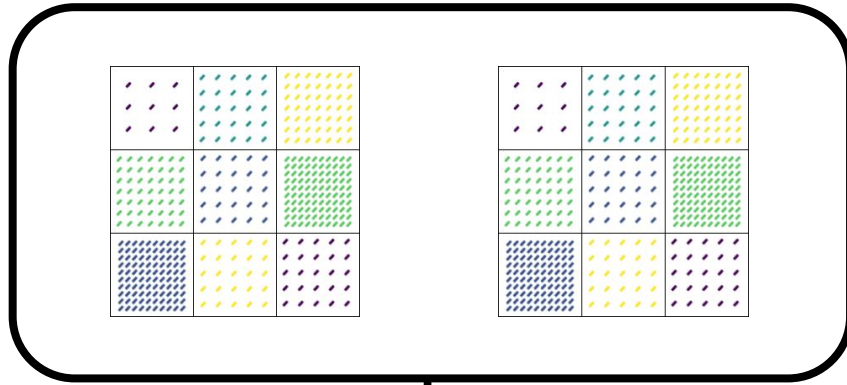
Attribute1	20
Attribute2	75
Attribute3	40
Attribute4	55



## 2. Directly Encode



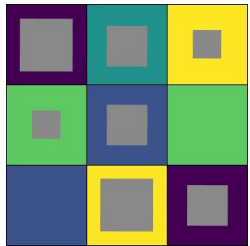
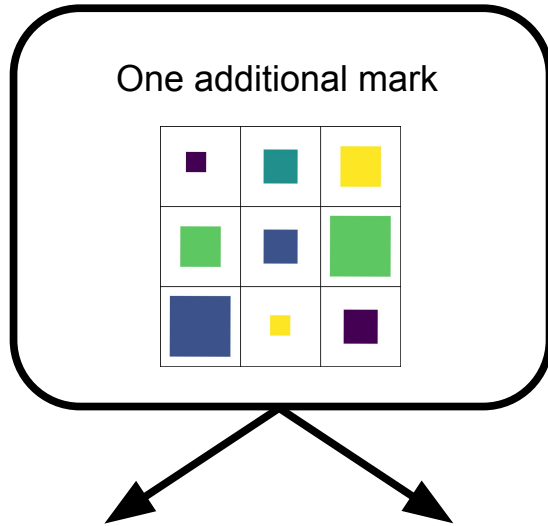
# Technique selection - Two overlaid marks



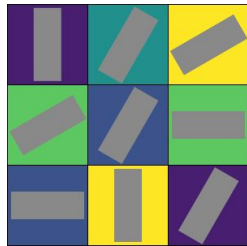
Bars

- Already used
- Length is a strong channel
- Separation between attributes

# Technique selection



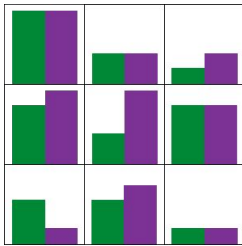
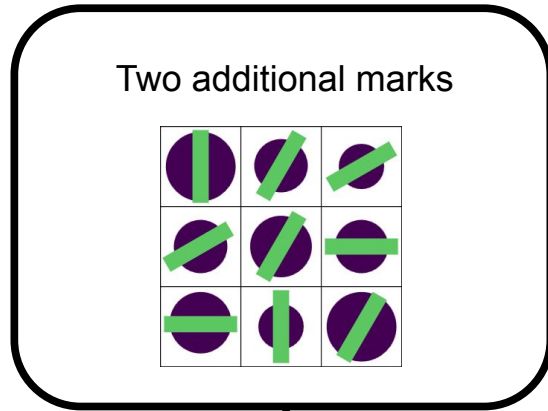
Mark size



Mark angle

- Same strategy, different channel for std
- Area, common channel
- Angle might benefit of the matrix grid
- Comparing them assess how mark channel affects performance

# Technique selection



Bars

- Already used
- Length is a strong channel
- Clear separation between attributes